Preliminary

- Traditionally, the subject of *Viscoelasticity* was all about measuring the *rheological properties* and the phenomenological theory of *Constitutive Equations.*
- This course will look more to the *dynamics of the flows.* In particular it will be interested in *Why* (a qualative understanding) and *How Much* (a quantitative understanding).
- The word *Rheology* was coined by Bingham in 1922 at Lafayette, with the assistance of a classics colleague.
- Two books
  - D.V. Boger & K. Walters, *Rheological Phenomena in Focus* (1993 Elsevier). NB: a picture book.
  - R.B. Bird, R.C. Armstrong & O. Hassager, *Dynamics of Polymeric Liquids, Vol. 1 Fluid Dynamics* (2nd edition, 1987, Wiley). NB 2nd edition much better than 1st. Vol 2 is dangerous. *NB: uses the pressure tensor* $= -\sigma$

Complex fluids

- What & where? tooth paste, soup, ketchup, synthetic fibres, plastic bags, anti-splat ink-jet printing, oil well drilling muds, DIY paints
- Why & when? micron microstructure: nano reacts in 10^{-9}s, time $\propto$ volume, so micron in 1s

More than: Viscous + Elastic

- Viscous:
  Bernoulli, lift, added mass, waves, boundary layers, stability, turbulence
- Elastic:
  structures, FE, waves, crack, composites
- Visco-elastic is more
  Not halfway between Viscous & Elastic – strange flows to explain

Lecture 1

Phenomena

Nonlinear flow

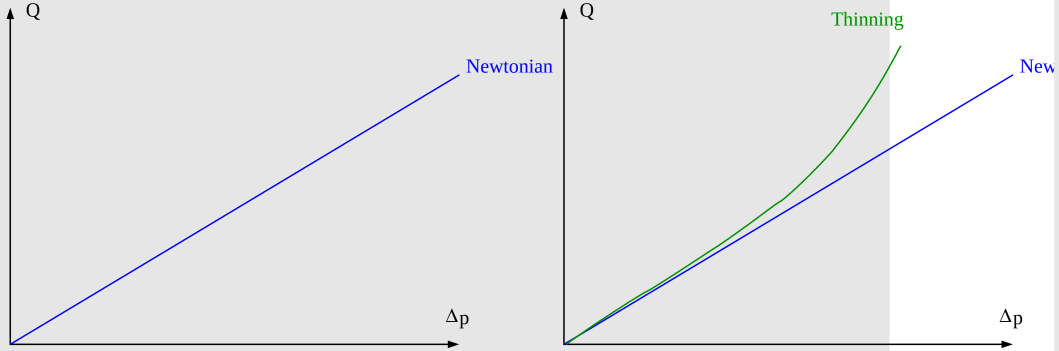
Inhibition of stretching

Elastic effects

Normal stress

Nonlinear flow

Flow down a pipe: flux Q, pressure drop Δp – just $\mu(\dot{\gamma})$



Thinning – more flow/less effort.
Breakdown of structure Thickenning – less flow/more effort.
Chaos & jamming Yield fluid – toothpaste, ketchup, non-drip paints,
particle transport Also 2D channel flow, as in injection molding,
coatings

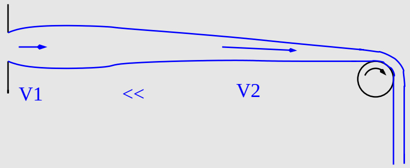
Nonlinear flow – summary

- Newtonian – linear flow.
- Thinning – more flow/less effort. Breakdown of structure
- Thickenning – less flow/more effort. Chaos & jamming
- Yield fluid – toothpaste, ketchup, non-drip paints, particle transport

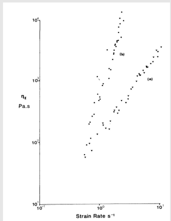
Also possible effects $\mu(p)$, and $\mu(T)$ with internal heating.

Inhibition of stretching

Spinline



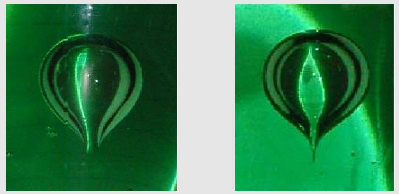
Extensional viscosity



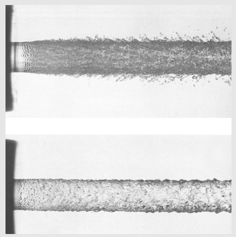
Large values compared to shear viscosity

Inhibition of stretching

Pointed bubbles



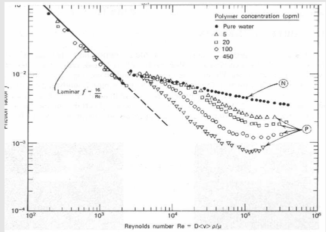
Smooth jets



Applications

Inhibition of stretching 2

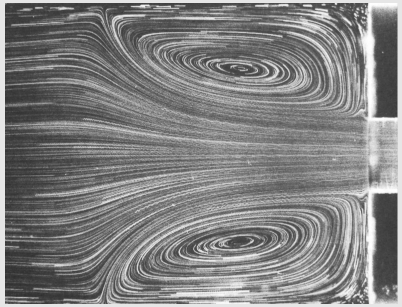
Reduction of turbulent drag



Application: 48km pipeline, flow 1.8m/s, 50% drag reduction by 9ppm of polymer
Application: Bristol Sewers, aircraft fuel

Inhibition of stretching 3

Long upstream vortices



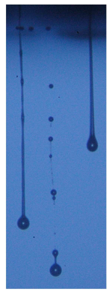
Uncontrolled output

Inhibition of stretching 4

Capillary squeezing of a liquid filament
very slow to break

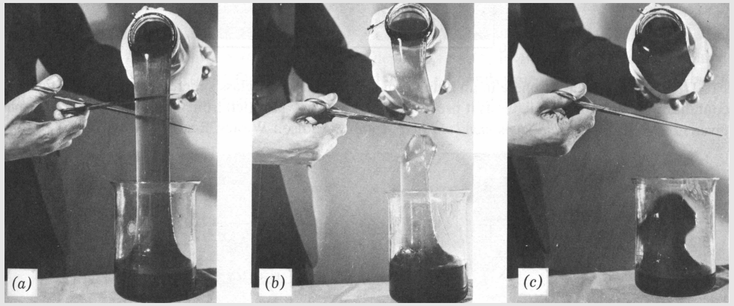
Inhibition of stretching 5

Drop-on-Demand Inkjet printing with too much polymer in ink



Elastic effects

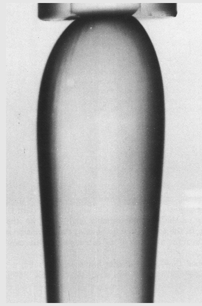
Recoil

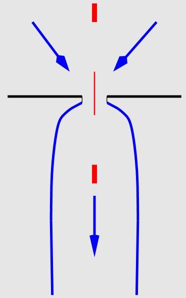


- also thick soup

Elastic effects 2

Die swell

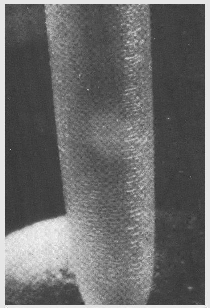




– recoil of fluid stretched in converging into hole

Elastic effects 3

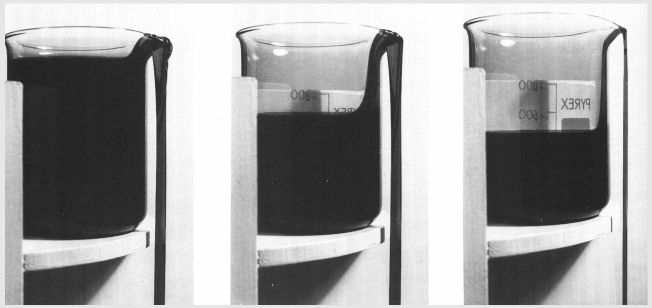
Die swell with ‘sharkskin’



May be a stick-slip effect?

Elastic effects 3

Open syphon

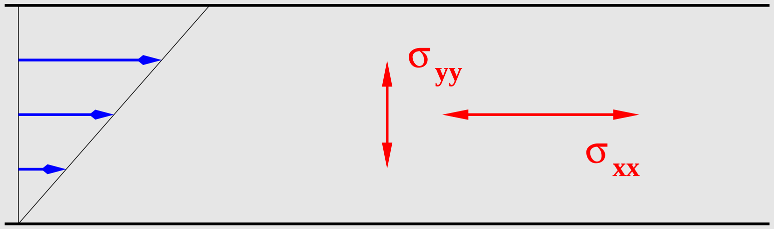


Find videos on web.

Normal stress

Simple shear flow

Normal stresses



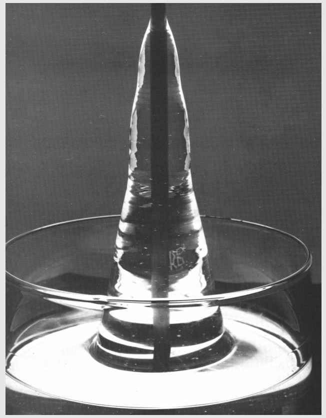
$\mathbf{u} = (\dot{\gamma} y, 0, 0)$

tension in streamlines

Sort of elastic stresses in shear flow

Normal stress 2

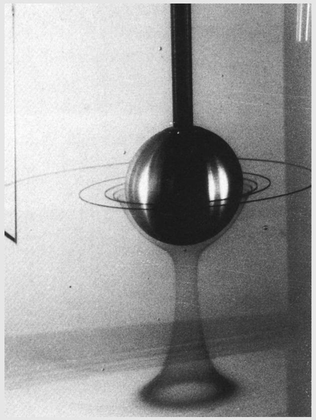
Rod climbing – Newtonian centrifuged out!



Fluid squeezed in by hoop stresses.

Normal stress 3

Secondary circulation for rotating sphere.

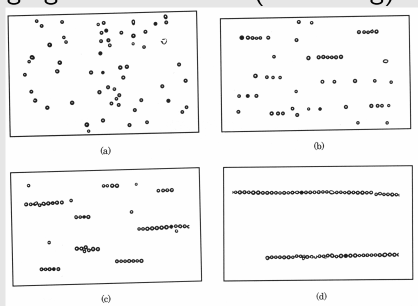


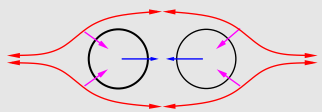
Same hoop stress effect.

Elastic effects always in opposite direction to inertial effects.

Normal stress 4

Agregation in time in (oscillating) shear.





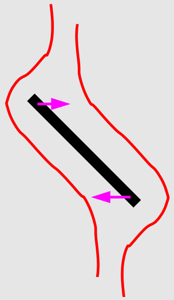
tension in streamlines

hoopstress effect

migration

Normal stress 5

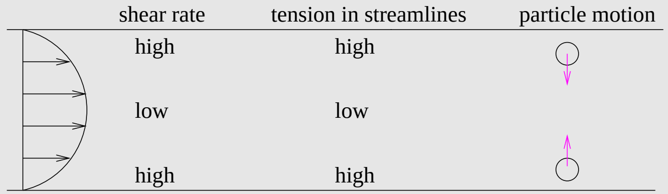
Sedimenting rods become vertical in an elastic liquid

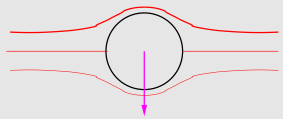


But become horizontal due to inertial effects

Normal stress 6

Migrate of particles to the centre line of pipe





Gradient in tension in streamline. Hoop stress force

Summary

Phenomena

Nonlinear flow
Inhibition of stretching
Elastic effects
Normal stress

No lecture Tuesday 25 January.
Next lecture Thursday 29 January.

Student Exercises: Find

- Open syphon video
- D.V. Boger & K. Walters, *Rheological Phenomena in Focus* (1993 Elsevier). NB: a picture book.
- R.B. Bird, R.C. Armstrong & O. Hassager, *Dynamics of Polymeric Liquids, Vol. 1 Fluid Dynamics* (2nd edition, 1987, Wiley). NB 2nd edition much better than 1st. Vol 2 is dangerous. *NB: uses the pressure tensor* $= -\sigma$