Core collapse in scalar-tensor theory of gravity

U. Sperhake

DAMTP, University of Cambridge



M. Horbatsch, H. Silva, D. Gerosa, P. Pani, R. Berti, L. Gualtieri, US arXiv:1505.07462

D. Gerosa, C. Ott, US work in preparation

III Amazonian Symposium on Physics, V NRHEP Meeting Belem, 02th October 2015







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Overview

- Introduction
- Formalism
- Neutron stars in bi-STT
- Core collapse in STT
- Conclusions

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1. Introduction

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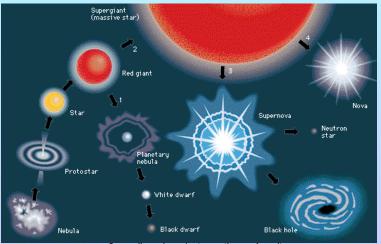
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Scalar-tensor theories of gravity

- Extra degree(s) of freedom ϕ^A additionally to $g_{\mu\nu}$
 - Appear in low-energy limit of string theories
 - Kaluza-Klein like models
 - Braneworld scenarios
- Historically: time-space dependent G_{Newton} Jordan '59, Fierz '56, Brans & Dicke '61
- Candidate for explaining the dark sector in cosmology, inflation
- Many alternative theories can be formulated as ST theories
- No-hair theorems for BHs
 - \Rightarrow matter sources often more sensitive to ST effects
 - E.g. spontaneous scalarization Damour & Esposito-Farese '93

The end of stellar evolution

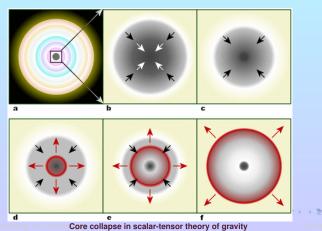
- Nuclear fusion above iron: energy consuming
- Stars with $M_{\rm ZAMS} \gtrsim 8~M_{\odot}$ explode as SN ightarrow NS, BH



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Core-collapse scenario (0th-order)

- $\bullet~$ Ni-Fe core reaches Chandrasekhar mass $\rightarrow~$ Collapse
- EOS stiffens at $\rho \gtrsim \rho_{\rm nuc} \rightarrow$ Bounce
- Outgoing shock, re-invigorated by $\nu_e \rightarrow$ Outer layers blast away



2. Formalism

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Notation

$arphi^{A}$	Scalar field(s)
γ_{AB}	Target space metric
$\gamma^{\mathcal{A}}_{\mathcal{BC}}$	Target space Christoffel symbols
$oldsymbol{g}_{\mu u}$	Physical spacetime metric
$ar{g}_{\mu u}$	Spacetime metric in the Einstein frame
ds ²	Physical line element
dīs²	Line element in the Einstein frame
$a\!(arphi^{\mathcal{A}})^2$	Conformal factor: $g_{\mu u}=a^2(arphi^{\mathcal{A}})ar{g}_{\mu u}$
$\partial_{\mathcal{A}}$	$\equiv rac{\partial}{\partial arphi^{\mathcal{A}}}$
In general:	bar \rightarrow Einstein frame variable
	no bar $ ightarrow$ Jordan frame variable
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Action and equations

cf. Damour & Esposito-Farese CQG 9, 2093

$$S = \frac{c^4}{4\pi\bar{G}} \int \frac{dx^4}{c} \sqrt{-\bar{g}} \left[\frac{\bar{R}}{4} - \frac{1}{2} \bar{g}^{\mu\nu} \gamma_{AB} (\partial_\mu \varphi^A) (\partial_\nu \varphi^B) + W(\varphi^A) \right] \\ + S_m [\psi_m, a^2(\varphi^A) \bar{g}_{\mu\nu}]$$

Energy momentum tensor: $T^{\mu\nu} = \frac{2}{\sqrt{-\bar{g}}} \frac{\delta S_m(\psi_m, g_{\mu\nu})}{\delta g_{\mu\nu}}$ $\bar{T}^{\mu\nu} = a^6 T^{\mu\nu}$

$$\Rightarrow \quad \bar{R}_{\mu\nu} = 2\gamma_{AB}(\partial_{\mu}\varphi^{A})(\partial_{\nu}\varphi^{B}) + 2W(\varphi^{A})\bar{g}_{\mu\nu} + \frac{8\pi\bar{G}}{c^{4}}\left(\bar{T}_{\mu\nu} - \frac{1}{2}\bar{T}_{\mu}\bar{\nu}\right)$$
$$\bar{\Box}\varphi^{A} = -\gamma^{A}_{BC}\bar{g}^{\mu\nu}(\partial_{\mu}\varphi^{B})(\partial_{\nu}\varphi^{C}) - \frac{4\pi\bar{G}}{c^{4}}\gamma^{AB}\frac{1}{a}(\partial_{B}a)\bar{T} + \gamma^{AB}\partial_{B}W$$
$$\bar{\nabla}_{\nu}\bar{T}^{\mu\nu} = \frac{1}{a}(\partial_{A}a)\bar{T}\bar{\nabla}^{\mu}\varphi^{A}$$

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Spherically symmetric stars

• Line element

 $ds^{2} = -\alpha^{2} dt^{2} + X^{2} dr^{2} + a^{2} r^{2} d\Omega^{2}, \quad d\bar{s}^{2} = -\bar{\alpha}^{2} dt^{2} + \bar{X}^{2} dr^{2} + r^{2} d\Omega^{2}$

Auxiliary variables

$$\bar{m} \equiv rac{r}{2} \left(1 - rac{a^2}{X^2}
ight) \,, \qquad \bar{\Phi} \equiv \ln \left(rac{lpha}{a}
ight) \,,$$

$$\eta^{A} = \frac{\partial_{r}\varphi^{A}}{X}, \quad \psi^{A} = \frac{\partial_{l}\varphi^{A}}{\alpha}, \quad \Xi = \gamma_{AB}(\eta^{A}\eta^{B} + \psi^{A}\psi^{B})$$

Matter

$$egin{aligned} & T_{lphaeta} = (\epsilon +
ho + m{
ho}) u_lpha u_eta + m{
ho} g_{lphaeta} \ & u^lpha = rac{1}{\sqrt{1-v^2}} \left[rac{1}{lpha}, \; rac{v}{X}, \; 0, \; 0
ight] \end{aligned}$$

 $J^{lpha} =
ho u^{lpha}$ "baryonic flow" satisfies $abla _{\mu} J^{\mu} = 0$

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Spherically symmetric stars

• Equation of state
$$P = K \rho^{\Gamma}$$
, $\epsilon = \frac{P}{\rho(\Gamma-1)}$

We typically use: $\Gamma = 2.34$, K = 1187 ($c = M_{\odot} = 1$)

EOS1 in Novak gr-qc/9707041

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Flux conservative variables

$$\begin{split} \bar{D} &= \frac{a^3 \rho X}{\sqrt{1 - v^2}} \\ \bar{S}^r &= \frac{a^4 [\rho(1 + \epsilon) + P] v}{1 - v^2} \\ \bar{\tau} &= \frac{a^4 [\rho(1 + \epsilon) + P]}{1 - v^2} - a^4 P - \bar{D} \end{split}$$

The equations: Metric and scalar field

•
$$\partial_r \Phi = \frac{X^2}{a^2} \left[\frac{\bar{m}}{r^2} + 4\pi r \left(\bar{S}^r v + a^4 P \right) + \frac{a^2 r}{2} \Xi \right],$$

 $\partial_r \bar{m} = 4\pi r^2 (\bar{\tau} + \bar{D}) + \frac{a^2 r^2}{2} \Xi,$
• $\partial_t \phi^A = \alpha \psi^A,$
 $\partial_t \eta^A = -\eta^A \frac{\partial_t X}{X} + \frac{\alpha}{X} \left(\partial_r \psi^A + \psi^A \frac{\partial_r \alpha}{\alpha} \right),$
 $\partial_t \psi^A = \frac{\alpha}{X} \left[\partial_r \eta^A + \frac{2}{r} \eta^A + \eta^A \frac{\partial_r \alpha}{\alpha} \right] - \psi^A \frac{\partial_t X}{X} - \alpha \gamma^A_{BC} (\psi^B \psi^C - \eta^B \eta^C) - 4\pi \alpha \left(\bar{\tau} - \bar{S}^r v + \bar{D} - 3a^4 P \right) \gamma^{AB} \frac{\partial_B a}{a^2}$

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The equations: Matter variables

•
$$\partial_t \bar{D} + \frac{a}{r^2} \partial_r \left(r^2 \frac{\alpha}{aX} f_{\bar{D}} \right) = s_{\bar{D}}, \qquad f_{\bar{D}} = \bar{D}v ,$$

 $\partial_t \bar{S}^r + \frac{1}{r^2} \partial_r \left(r^2 \frac{\alpha}{X} f_{\bar{S}^r} \right) = s_{\bar{S}^r}, \qquad f_{\bar{S}^r} = \bar{S}^r v + a^4 P ,$
 $\partial_t \bar{\tau} + \frac{1}{r^2} \partial_r \left(r^2 \frac{\alpha}{X} f_{\bar{\tau}} \right) = s_{\bar{\tau}}, \qquad f_{\bar{\tau}} = \bar{S}^r - \bar{D}v .$

- Flux conservative form! The source terms $s_{\overline{D}}$, $s_{\overline{S}^r}$, $s_{\overline{\tau}}$ contain no derivatives.
- Suitable for high-resolution shock-capturing methods extension of GR1D O'Connor & Ott 0912:2393 [astro-ph]

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The static limit \rightarrow TOV models, initial data

- All time derivatives vanish
- Relation $(\bar{D}, \bar{S}^r, \bar{\tau}) \leftrightarrow (\rho, \epsilon, v)$ trivial as v = 0

- Gives system of 5 ODEs for $(\alpha, X, P, \varphi^A, \eta^A)$
- Boundary conditions
 - At r = 0: X = 1, $\rho = \rho_c$, $\eta^A = 0$

At $r = r_S$: P = 0

At $r \to \infty$: $\varphi^{A} = 0$ (wlog)

3. Neutron stars in multi-ST theories

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Specifying the theory

Target geometry: maximally symmetric

$$\gamma_{AB} = \delta_{AB} \left[1 + \frac{(\varphi^1)^2 + (\varphi^2)^2}{4r^2} \right] \qquad \text{spherical:} \quad r^2 > 0$$

hyperbolic: $r^2 < 0$
flat: $r^2 \to \infty$

Conformal factor

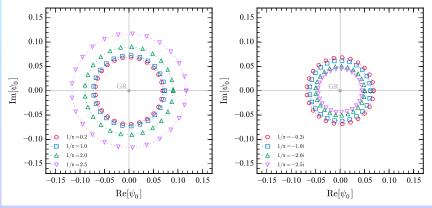
 $\log a = 2\alpha_0\varphi^1 - 2\alpha_1\varphi^2 + \frac{1}{2}(\beta_0 + \beta_1)(\varphi^1)^2 + \frac{1}{2}(\beta_0 - \beta_1)(\varphi^2)^2$

• Complex scalar field: $\varphi = \varphi^1 + i\varphi^2$

• Free parameters: $\alpha_0, \alpha_1, \beta_0, \beta_1, r$

Case 1: $\alpha_0 = \alpha_1 = \beta_1 = 0$, $\beta_0 = -5$

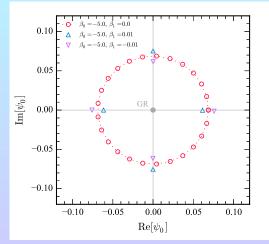
- O(2) symmetry: Invariance under rotation in φ^1, φ^2 plane
- Spherical (hyperbolic) target geometry
 - \Rightarrow scalarization strengthened (weakened)



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Case 2: $\alpha_0 = \alpha_1 = 0$, $\beta_0 = -5$, $\beta_1 \neq 0$

• No bi-scalarized solutions! "Circle" \rightarrow "Cross" • r = 5



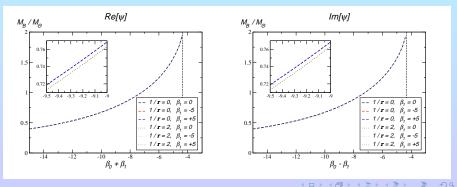
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Case 2: Scalarization for $\beta_0 \pm \beta_1 \lesssim -4.35$

• Spontaneous scalarization for single-STT if $\beta \lesssim -4.35$

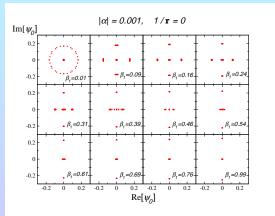
Damour & Esposito-Farese '93

• Here: $\log a = 2\alpha_0\varphi^1 - 2\alpha_1\varphi^2 + \frac{1}{2}(\beta_0 + \beta_1)(\varphi^1)^2 + \frac{1}{2}(\beta_0 - \beta_1)(\varphi^2)^2$ \rightarrow Like single-STT with $\beta \rightarrow \beta_0 \pm \beta_1$



Case 3: $(\alpha_0, \alpha_1) \neq 0$, $\beta_0 = -5$

- $\alpha \equiv |(\alpha_0, \alpha_1)|$ constrained; But phase not!
- $\alpha \neq$ 0 facilitates bi-scalar solutions

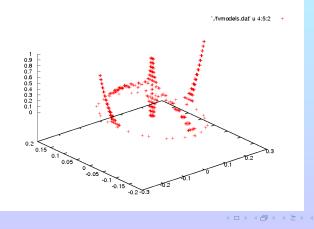


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Case 3: $(\alpha_0, \alpha_1) \neq 0$, $\beta_0 = -5$

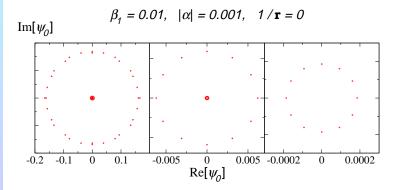
- $\alpha \equiv |(\alpha_0, \alpha_1)|$ constrained; But phase not!
- $\alpha \neq$ 0 facilitates bi-scalar solutions



Case 3: $(\alpha_0, \alpha_1) \neq 0$, $\beta_0 = -5$

• Zoom into upper left panel of above ($\beta_1 = 0.01$)

• Fine structure of (weakly) scalarized solutions



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4. Core collapse in single-ST theories

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Core collapse

- Massive stars: $M_{ZAMS} \approx 8 \dots 100 M_{\odot}$
- Core compressed from $\sim 1500~{\rm km}$ to $\sim 15~{\rm km}$ $\sim 10^{10}~{\rm g/cm^3} ~{\rm to} \sim > 10^{15}~{\rm g/cm^3}$
- Released gravitational energy: $O(10^{53})$ erg ~ 99 % in neutrinos, ~ 10⁵¹ erg in outgoing shock, explosion

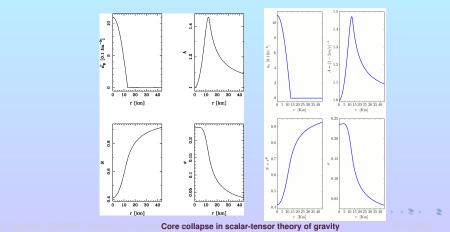
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- Explosion mechanism: still uncertainties...
- Failed explosion ⇒ BH formation
 Collapsar possible engine for long-soft GRB

Code test: Static NS models

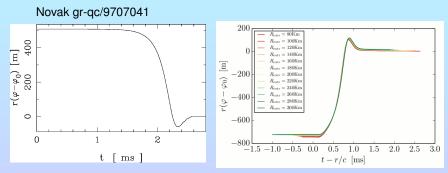
• $\bar{M} = 2.4 \ M_{\odot}, \ \bar{R} = 13.1 \ {
m km}$ model with $\alpha_0 = 0, \ \beta_0 = -6$ Novak gr-qc/9707041

• Baryon density, metric functions, scalar field



Code test: NS collapse to BH

- Intial model: $\bar{R} = 11.8 \text{ km}, \ \bar{M} = 2.07 M_{\odot}$
- $\alpha_0 = 0.0025, \quad \beta_0 = -5$

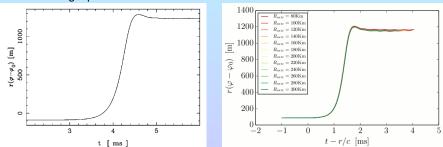


- Discrepancy due to sign error in α₀ in Novak
- As $\alpha_0 \rightarrow 0$, we agree with Novak

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Code test: Transition from GR to scalarized star

- Unstable GR-like model: $\bar{R} = 13.2 \text{ km}, \quad \bar{M} = 1.378 \text{ } M_{\odot}$
- ... migrates to scalarized model: $\bar{R} = 13.0 \text{ km}$, $M = 1.373 M_{\odot}$
- Here: $\alpha_0 = 0.01$, $\beta_0 = -6$



Novak gr-qc/9806022

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Core collapse: Hybrid EOS

- Model stiffening of EOS through change in polytropic index
- $P = P_{cold} + P_{thermal}$ where $P_{cold} = Polytrope(\Gamma_1, \Gamma_2)$ matched at $\rho = \rho_{nuc}$ $P_{thermal} = (\Gamma_{th} - 1)\rho(\epsilon - \epsilon_0)$
- Before shock formation: $\epsilon = \epsilon_0$
 - \rightarrow *P*_{thermal} models non-adiabatic shock flow
- We use $\Gamma_1 = 1.3$, $\Gamma_2 = 2.5$, $\Gamma_{th} = 1.25 \dots 1.5$

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Presupernova model: s12WH2007

 From stellar evolution codes up to the onset of core collapse Woosley & Heger Phys.Rep.442, 269

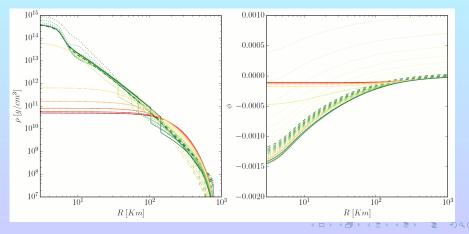
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Solar metalicity

- ZAMS mass $M = 12 \ M_{\odot} \gtrsim M_{\rm pre-SN}$
- Generated with Newtonian gravity
- Set $\alpha_0 \neq 0$ to trigger scalar field

Core bounce

- ρ , φ profiles at different *t*
- Core bounce \Rightarrow outgoing shock

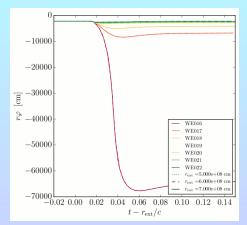


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Wave signal: Varying Γ_{th} ; $\alpha_0 = 0.01$, $\beta_0 = -5$

- Extra pressure $\propto \Gamma_{th}$
- Small Γ_{th}
 - \Rightarrow more massive NS
 - ⇒ Spontaneous scalarization
- Similar to WD collapse
 Novak & Ibañez astro-ph/9911298
- Detectable to ~ 1 Mpc
 But depends on α₀!!



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5. Conclusions

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Conclusions

- Formalism for multi-scalar theories similar to single ST
- For $\alpha_0 = 0$, effectively like ST
- Bi-scalarized solutions require $\alpha_0 \neq 0$
- Complex structure in $(\varphi_c^1, \varphi_c^2)$ plane
- Core collapse in spherical symmetry
- Code tested successfully; identified few typos in literature
- Core bounce dynamics so far similar to GR
- Scalar waveforms strongly dependent on EOS Detectability $\propto \alpha_0$

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