# Core collapse in scalar-tensor theory of gravity

#### U. Sperhake

DAMTP, University of Cambridge



M. Horbatsch, H. Silva, D. Gerosa, P. Pani, R. Berti, L. Gualtieri, US arXiv:1505.07462

D. Gerosa, C. Ott, US work in preparation

III Amazonian Symposium on Physics, V NRHEP Meeting Belem, 02<sup>th</sup> October 2015







U. Sperhake (DAMTP, University of Cambr Core collapse in scalar-tensor theory of gravity

02/10/2015 1 / 3

#### Overview

- Introduction
- Formalism
- Neutron stars in bi-STT
- Core collapse in STT
- Conclusions

イロト イポト イヨト イヨト

# 1. Introduction

U. Sperhake (DAMTP, University of Cambri Core collapse in scalar-tensor theory of gravity

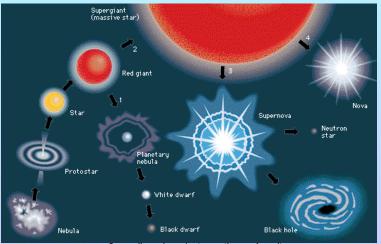
02/10/2015 3 / 33

### Scalar-tensor theories of gravity

- Extra degree(s) of freedom  $\phi^A$  additionally to  $g_{\mu\nu}$ 
  - Appear in low-energy limit of string theories
  - Kaluza-Klein like models
  - Braneworld scenarios
- Historically: time-space dependent G<sub>Newton</sub> Jordan '59, Fierz '56, Brans & Dicke '61
- Candidate for explaining the dark sector in cosmology, inflation
- Many alternative theories can be formulated as ST theories
- No-hair theorems for BHs
  - $\Rightarrow$  matter sources often more sensitive to ST effects
  - E.g. spontaneous scalarization Damour & Esposito-Farese '93

#### The end of stellar evolution

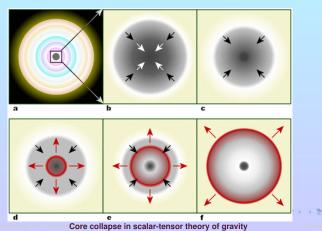
- Nuclear fusion above iron: energy consuming
- Stars with  $M_{\rm ZAMS} \gtrsim 8~M_{\odot}$  explode as SN ightarrow NS, BH



Core collapse in scalar-tensor theory of gravity

#### Core-collapse scenario (0<sup>th</sup>-order)

- $\bullet~$  Ni-Fe core reaches Chandrasekhar mass  $\rightarrow~$  Collapse
- EOS stiffens at  $\rho \gtrsim \rho_{\rm nuc} \rightarrow$  Bounce
- Outgoing shock, re-invigorated by  $\nu_e \rightarrow$  Outer layers blast away



# 2. Formalism

U. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

02/10/2015 7 / 33

・ロト ・ 同 ト ・ ヨ ト ・ ヨ ト … ヨ

# Notation

$arphi^{A}$	Scalar field(s)
$\gamma_{AB}$	Target space metric
$\gamma^{\mathcal{A}}_{\mathcal{BC}}$	Target space Christoffel symbols
$oldsymbol{g}_{\mu u}$	Physical spacetime metric
$ar{g}_{\mu u}$	Spacetime metric in the Einstein frame
ds <sup>2</sup>	Physical line element
dīs²	Line element in the Einstein frame
$a\!(arphi^{\mathcal{A}})^2$	Conformal factor: $g_{\mu u}=a^2(arphi^{\mathcal{A}})ar{g}_{\mu u}$
$\partial_{\mathcal{A}}$	$\equiv rac{\partial}{\partial arphi^{\mathcal{A}}}$
In general:	bar $\rightarrow$ Einstein frame variable
	no bar $ ightarrow$ Jordan frame variable
	<ロ><団><日><三

#### Action and equations

cf. Damour & Esposito-Farese CQG 9, 2093

$$S = \frac{c^4}{4\pi\bar{G}} \int \frac{dx^4}{c} \sqrt{-\bar{g}} \left[ \frac{\bar{R}}{4} - \frac{1}{2} \bar{g}^{\mu\nu} \gamma_{AB} (\partial_\mu \varphi^A) (\partial_\nu \varphi^B) + W(\varphi^A) \right] \\ + S_m [\psi_m, a^2(\varphi^A) \bar{g}_{\mu\nu}]$$

Energy momentum tensor:  $T^{\mu\nu} = \frac{2}{\sqrt{-\bar{g}}} \frac{\delta S_m(\psi_m, g_{\mu\nu})}{\delta g_{\mu\nu}}$  $\bar{T}^{\mu\nu} = a^6 T^{\mu\nu}$ 

$$\Rightarrow \quad \bar{R}_{\mu\nu} = 2\gamma_{AB}(\partial_{\mu}\varphi^{A})(\partial_{\nu}\varphi^{B}) + 2W(\varphi^{A})\bar{g}_{\mu\nu} + \frac{8\pi\bar{G}}{c^{4}}\left(\bar{T}_{\mu\nu} - \frac{1}{2}\bar{T}_{\mu}\bar{\nu}\right)$$
$$\bar{\Box}\varphi^{A} = -\gamma^{A}_{BC}\bar{g}^{\mu\nu}(\partial_{\mu}\varphi^{B})(\partial_{\nu}\varphi^{C}) - \frac{4\pi\bar{G}}{c^{4}}\gamma^{AB}\frac{1}{a}(\partial_{B}a)\bar{T} + \gamma^{AB}\partial_{B}W$$
$$\bar{\nabla}_{\nu}\bar{T}^{\mu\nu} = \frac{1}{a}(\partial_{A}a)\bar{T}\bar{\nabla}^{\mu}\varphi^{A}$$

U. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

02/10/2015 9 / 33

#### Spherically symmetric stars

• Line element

 $ds^{2} = -\alpha^{2} dt^{2} + X^{2} dr^{2} + a^{2} r^{2} d\Omega^{2}, \quad d\bar{s}^{2} = -\bar{\alpha}^{2} dt^{2} + \bar{X}^{2} dr^{2} + r^{2} d\Omega^{2}$ 

Auxiliary variables

$$\bar{m} \equiv rac{r}{2} \left( 1 - rac{a^2}{X^2} 
ight) \,, \qquad \bar{\Phi} \equiv \ln \left( rac{lpha}{a} 
ight) \,,$$

$$\eta^{A} = \frac{\partial_{r}\varphi^{A}}{X}, \quad \psi^{A} = \frac{\partial_{l}\varphi^{A}}{\alpha}, \quad \Xi = \gamma_{AB}(\eta^{A}\eta^{B} + \psi^{A}\psi^{B})$$

Matter

$$egin{aligned} & T_{lphaeta} = (\epsilon + 
ho + m{
ho}) u_lpha u_eta + m{
ho} g_{lphaeta} \ & u^lpha = rac{1}{\sqrt{1-v^2}} \left[rac{1}{lpha}, \; rac{v}{X}, \; 0, \; 0
ight] \end{aligned}$$

 $J^{lpha} = 
ho u^{lpha}$  "baryonic flow" satisfies  $abla _{\mu} J^{\mu} = 0$ 

J. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

#### Spherically symmetric stars

• Equation of state 
$$P = K \rho^{\Gamma}$$
,  $\epsilon = \frac{P}{\rho(\Gamma-1)}$ 

We typically use:  $\Gamma = 2.34$ , K = 1187 ( $c = M_{\odot} = 1$ )

EOS1 in Novak gr-qc/9707041

イロト イポト イヨト イヨト

Flux conservative variables

$$\begin{split} \bar{D} &= \frac{a^3 \rho X}{\sqrt{1 - v^2}} \\ \bar{S}^r &= \frac{a^4 [\rho(1 + \epsilon) + P] v}{1 - v^2} \\ \bar{\tau} &= \frac{a^4 [\rho(1 + \epsilon) + P]}{1 - v^2} - a^4 P - \bar{D} \end{split}$$

#### The equations: Metric and scalar field

• 
$$\partial_r \Phi = \frac{X^2}{a^2} \left[ \frac{\bar{m}}{r^2} + 4\pi r \left( \bar{S}^r v + a^4 P \right) + \frac{a^2 r}{2} \Xi \right],$$
  
 $\partial_r \bar{m} = 4\pi r^2 (\bar{\tau} + \bar{D}) + \frac{a^2 r^2}{2} \Xi,$   
•  $\partial_t \phi^A = \alpha \psi^A,$   
 $\partial_t \eta^A = -\eta^A \frac{\partial_t X}{X} + \frac{\alpha}{X} \left( \partial_r \psi^A + \psi^A \frac{\partial_r \alpha}{\alpha} \right),$   
 $\partial_t \psi^A = \frac{\alpha}{X} \left[ \partial_r \eta^A + \frac{2}{r} \eta^A + \eta^A \frac{\partial_r \alpha}{\alpha} \right] - \psi^A \frac{\partial_t X}{X} - \alpha \gamma^A_{BC} (\psi^B \psi^C - \eta^B \eta^C) - 4\pi \alpha \left( \bar{\tau} - \bar{S}^r v + \bar{D} - 3a^4 P \right) \gamma^{AB} \frac{\partial_B a}{a^2}$ 

U. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

02/10/2015 12 / 3

<ロ> <同> <同> <同> <同> < 同>

#### The equations: Matter variables

• 
$$\partial_t \bar{D} + \frac{a}{r^2} \partial_r \left( r^2 \frac{\alpha}{aX} f_{\bar{D}} \right) = s_{\bar{D}}, \qquad f_{\bar{D}} = \bar{D}v ,$$
  
 $\partial_t \bar{S}^r + \frac{1}{r^2} \partial_r \left( r^2 \frac{\alpha}{X} f_{\bar{S}^r} \right) = s_{\bar{S}^r}, \qquad f_{\bar{S}^r} = \bar{S}^r v + a^4 P ,$   
 $\partial_t \bar{\tau} + \frac{1}{r^2} \partial_r \left( r^2 \frac{\alpha}{X} f_{\bar{\tau}} \right) = s_{\bar{\tau}}, \qquad f_{\bar{\tau}} = \bar{S}^r - \bar{D}v .$ 

- Flux conservative form! The source terms  $s_{\overline{D}}$ ,  $s_{\overline{S}^r}$ ,  $s_{\overline{\tau}}$  contain no derivatives.
- Suitable for high-resolution shock-capturing methods extension of GR1D O'Connor & Ott 0912:2393 [astro-ph]

・ロット (雪) (日) (日)

#### The static limit $\rightarrow$ TOV models, initial data

- All time derivatives vanish
- Relation  $(\bar{D}, \bar{S}^r, \bar{\tau}) \leftrightarrow (\rho, \epsilon, v)$  trivial as v = 0

- Gives system of 5 ODEs for  $(\alpha, X, P, \varphi^A, \eta^A)$
- Boundary conditions
  - At r = 0: X = 1,  $\rho = \rho_c$ ,  $\eta^A = 0$

At  $r = r_S$ : P = 0

At  $r \to \infty$ :  $\varphi^{A} = 0$  (wlog)

# 3. Neutron stars in multi-ST theories

U. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

02/10/2015 15 / 33

ヘロト ヘヨト ヘヨト ヘヨ

## Specifying the theory

Target geometry: maximally symmetric

$$\gamma_{AB} = \delta_{AB} \left[ 1 + \frac{(\varphi^1)^2 + (\varphi^2)^2}{4r^2} \right] \qquad \text{spherical:} \quad r^2 > 0$$
  
hyperbolic:  $r^2 < 0$   
flat:  $r^2 \to \infty$ 

Conformal factor

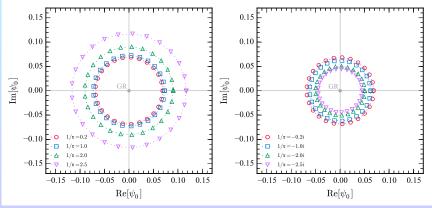
 $\log a = 2\alpha_0\varphi^1 - 2\alpha_1\varphi^2 + \frac{1}{2}(\beta_0 + \beta_1)(\varphi^1)^2 + \frac{1}{2}(\beta_0 - \beta_1)(\varphi^2)^2$ 

• Complex scalar field:  $\varphi = \varphi^1 + i\varphi^2$ 

• Free parameters:  $\alpha_0, \alpha_1, \beta_0, \beta_1, r$ 

#### Case 1: $\alpha_0 = \alpha_1 = \beta_1 = 0$ , $\beta_0 = -5$

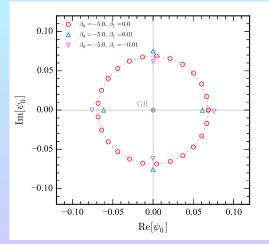
- O(2) symmetry: Invariance under rotation in  $\varphi^1, \varphi^2$  plane
- Spherical (hyperbolic) target geometry
  - $\Rightarrow$  scalarization strengthened (weakened)



Core collapse in scalar-tensor theory of gravity

#### Case 2: $\alpha_0 = \alpha_1 = 0$ , $\beta_0 = -5$ , $\beta_1 \neq 0$

• No bi-scalarized solutions! "Circle"  $\rightarrow$  "Cross" • r = 5



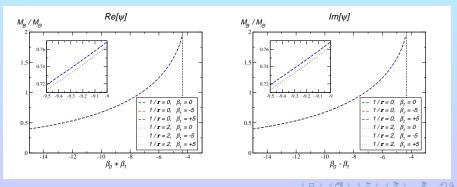
U. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

#### Case 2: Scalarization for $\beta_0 \pm \beta_1 \lesssim -4.35$

• Spontaneous scalarization for single-STT if  $\beta \lesssim -4.35$ 

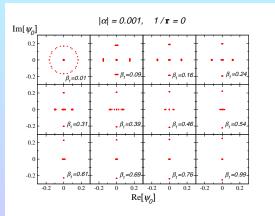
Damour & Esposito-Farese '93

• Here:  $\log a = 2\alpha_0\varphi^1 - 2\alpha_1\varphi^2 + \frac{1}{2}(\beta_0 + \beta_1)(\varphi^1)^2 + \frac{1}{2}(\beta_0 - \beta_1)(\varphi^2)^2$  $\rightarrow$  Like single-STT with  $\beta \rightarrow \beta_0 \pm \beta_1$ 



## Case 3: $(\alpha_0, \alpha_1) \neq 0$ , $\beta_0 = -5$

- $\alpha \equiv |(\alpha_0, \alpha_1)|$  constrained; But phase not!
- $\alpha \neq$  0 facilitates bi-scalar solutions

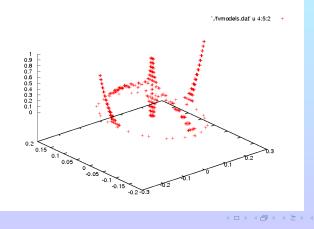


U.Spechake (DAMTR) University of CambriCore collapse in scalar-tensor theory of gravity

- E - E

# Case 3: $(\alpha_0, \alpha_1) \neq 0$ , $\beta_0 = -5$

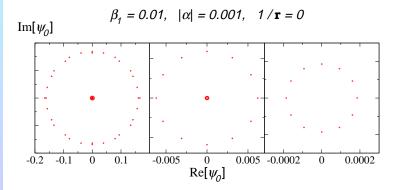
- $\alpha \equiv |(\alpha_0, \alpha_1)|$  constrained; But phase not!
- $\alpha \neq$  0 facilitates bi-scalar solutions



# Case 3: $(\alpha_0, \alpha_1) \neq 0$ , $\beta_0 = -5$

• Zoom into upper left panel of above ( $\beta_1 = 0.01$ )

• Fine structure of (weakly) scalarized solutions



)2/10/2015 22/

# 4. Core collapse in single-ST theories

U. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

02/10/2015 23 / 33

#### Core collapse

- Massive stars:  $M_{ZAMS} \approx 8 \dots 100 M_{\odot}$
- Core compressed from  $\sim 1500~{\rm km}$  to  $\sim 15~{\rm km}$   $\sim 10^{10}~{\rm g/cm^3} ~{\rm to} \sim > 10^{15}~{\rm g/cm^3}$
- Released gravitational energy:  $O(10^{53})$  erg ~ 99 % in neutrinos, ~ 10<sup>51</sup> erg in outgoing shock, explosion

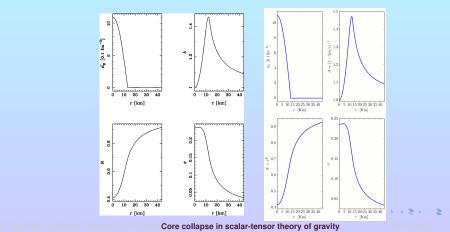
・ロト・西ト・ヨト・ヨト ヨー うのの

- Explosion mechanism: still uncertainties...
- Failed explosion ⇒ BH formation
   Collapsar possible engine for long-soft GRB

#### Code test: Static NS models

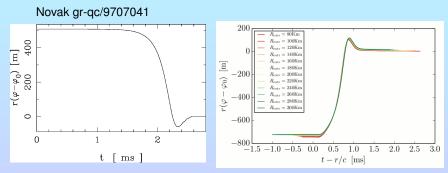
•  $\bar{M} = 2.4 \ M_{\odot}, \ \bar{R} = 13.1 \ {
m km}$  model with  $\alpha_0 = 0, \ \beta_0 = -6$ Novak gr-qc/9707041

• Baryon density, metric functions, scalar field



#### Code test: NS collapse to BH

- Intial model:  $\bar{R} = 11.8 \text{ km}, \ \bar{M} = 2.07 M_{\odot}$
- $\alpha_0 = 0.0025, \quad \beta_0 = -5$

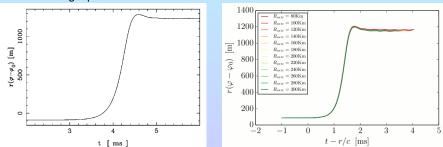


- Discrepancy due to sign error in α<sub>0</sub> in Novak
- As  $\alpha_0 \rightarrow 0$ , we agree with Novak

U. Sperhake (DAMTP, University of Cambr Core collapse in scalar-tensor theory of gravity

#### Code test: Transition from GR to scalarized star

- Unstable GR-like model:  $\bar{R} = 13.2 \text{ km}, \quad \bar{M} = 1.378 \text{ } M_{\odot}$
- ... migrates to scalarized model:  $\bar{R} = 13.0 \text{ km}$ ,  $M = 1.373 M_{\odot}$
- Here:  $\alpha_0 = 0.01$ ,  $\beta_0 = -6$



Novak gr-qc/9806022

U. Spechake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

(I)

### Core collapse: Hybrid EOS

- Model stiffening of EOS through change in polytropic index
- $P = P_{cold} + P_{thermal}$  where  $P_{cold} = Polytrope(\Gamma_1, \Gamma_2)$  matched at  $\rho = \rho_{nuc}$  $P_{thermal} = (\Gamma_{th} - 1)\rho(\epsilon - \epsilon_0)$
- Before shock formation:  $\epsilon = \epsilon_0$ 
  - $\rightarrow$  *P*<sub>thermal</sub> models non-adiabatic shock flow
- We use  $\Gamma_1 = 1.3$ ,  $\Gamma_2 = 2.5$ ,  $\Gamma_{th} = 1.25 \dots 1.5$

・ロ・・ 日・ ・ ヨ・ ・ ヨ・ ・ りゅつ

## Presupernova model: s12WH2007

 From stellar evolution codes up to the onset of core collapse Woosley & Heger Phys.Rep.442, 269

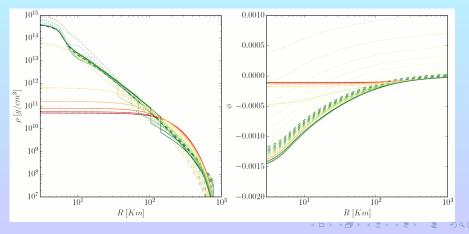
・ロット (雪) (日) (日) 日

Solar metalicity

- ZAMS mass  $M = 12 \ M_{\odot} \gtrsim M_{\rm pre-SN}$
- Generated with Newtonian gravity
- Set  $\alpha_0 \neq 0$  to trigger scalar field

#### Core bounce

- $\rho$ ,  $\varphi$  profiles at different *t*
- Core bounce  $\Rightarrow$  outgoing shock

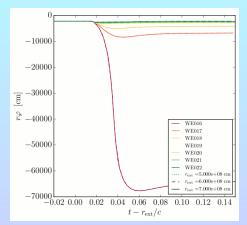


U. Sperhake (DAMTP, University of Cambri Core collapse in scalar-tensor theory of gravity



# Wave signal: Varying $\Gamma_{th}$ ; $\alpha_0 = 0.01$ , $\beta_0 = -5$

- Extra pressure  $\propto \Gamma_{th}$
- Small Γ<sub>th</sub>
  - $\Rightarrow$  more massive NS
  - ⇒ Spontaneous scalarization
- Similar to WD collapse
   Novak & Ibañez astro-ph/9911298
- Detectable to ~ 1 Mpc
   But depends on α<sub>0</sub>!!



< ロ > < 同 > < 回 > < 回 >

U. Sperhake (DAMTP, University of Cambr Core collapse in scalar-tensor theory of gravity

# 5. Conclusions

U. Sperhake (DAMTP, University of CambriCore collapse in scalar-tensor theory of gravity

02/10/2015 32 / 33

<ロ> <同> <同> < 同> < 同> < 同> < 同><</p>

#### Conclusions

- Formalism for multi-scalar theories similar to single ST
- For  $\alpha_0 = 0$ , effectively like ST
- Bi-scalarized solutions require  $\alpha_0 \neq 0$
- Complex structure in  $(\varphi_c^1, \varphi_c^2)$  plane
- Core collapse in spherical symmetry
- Code tested successfully; identified few typos in literature
- Core bounce dynamics so far similar to GR
- Scalar waveforms strongly dependent on EOS Detectability  $\propto \alpha_0$

U. Sperhake (DAMTP, University of Cambri Core collapse in scalar-tensor theory of gravity